Advanced KEM Concepts

(Hybrid) Obfuscation and Verifiable Decapsulation



IBM Research Europe – Zurich

based on work with

Lewis Glabush EPFL Kathrin Hövelmanns
TU Eindhoven

Michael Rosenberg
Cloudflare

Douglas StebilaU Waterloo

Shannon Veitch

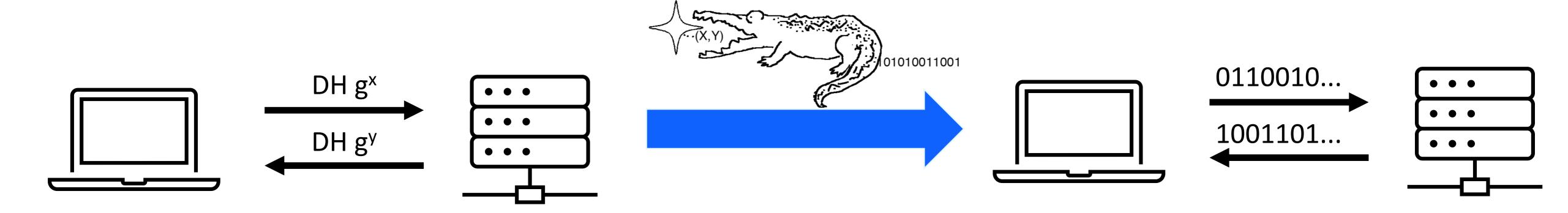
ETH Zurich



Protocol Obfuscation

Internet protocols hide metadata to protect user privacy, dissuade protocol fingerprinting, and prevent network ossification

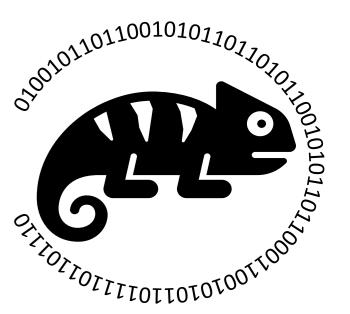
- TLS 1.3 Encrypted Client Hello, QUIC, pseudorandom cTLS, obfs4, Shadowsocks, ...
- "Fully-encrypted" protocols, with **obfuscated** key exchange



Quantum-safe transition?

ML-KEM public keys and ciphertexts don't look random!

Kemeleon



ML-KEM/Kyber public keys

- vector of coefficients mod q = 3329

[
$$a_1$$
][a_2][a_3]...[a_b] $a_i \in \mathbb{Z}_q = \{0, \ldots, 3328\}$ - each a_i represented in 12 bits

most sig. bit of each value biased towards 0

- Encoding for public keys:
 - 1. accumulate into one big number
 - 2. rejection sampling: reject if msb is 1

[
$$A = a_1 + a_2 \cdot q + a_3 \cdot q^2 + \cdots + a_b \cdot q^{b-1}$$
]

most sig. bit still biased towards 0

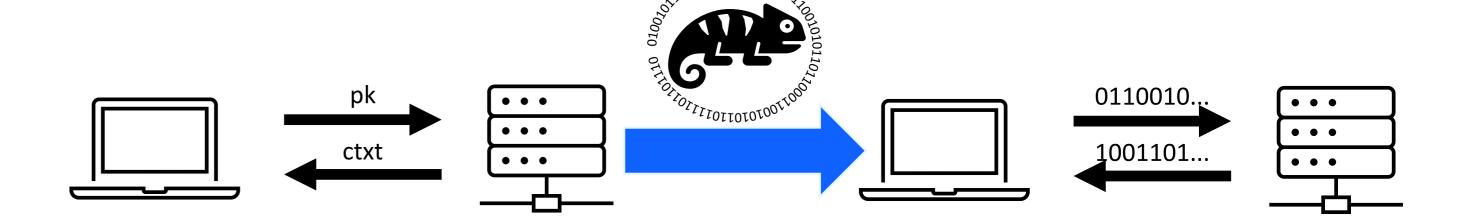
Encoded public keys ~2.5% smaller than regular (-19/28/38 bytes for ML-KEM-512/768/1024)

ML-KEM-768 likelihood of rejection is ~17%

ML-KEM/Kyber ciphertexts

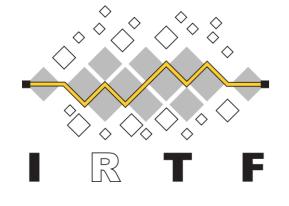
- vector of compressed coefficients need to first "decompress"
- encoded ciphertexts larger than regular (6–15%)

Obfuscated KEMs



ML-KEM

- + Kemeleon public key and ciphertext encoding
- = Obfuscated KEM: ML-Kemeleon



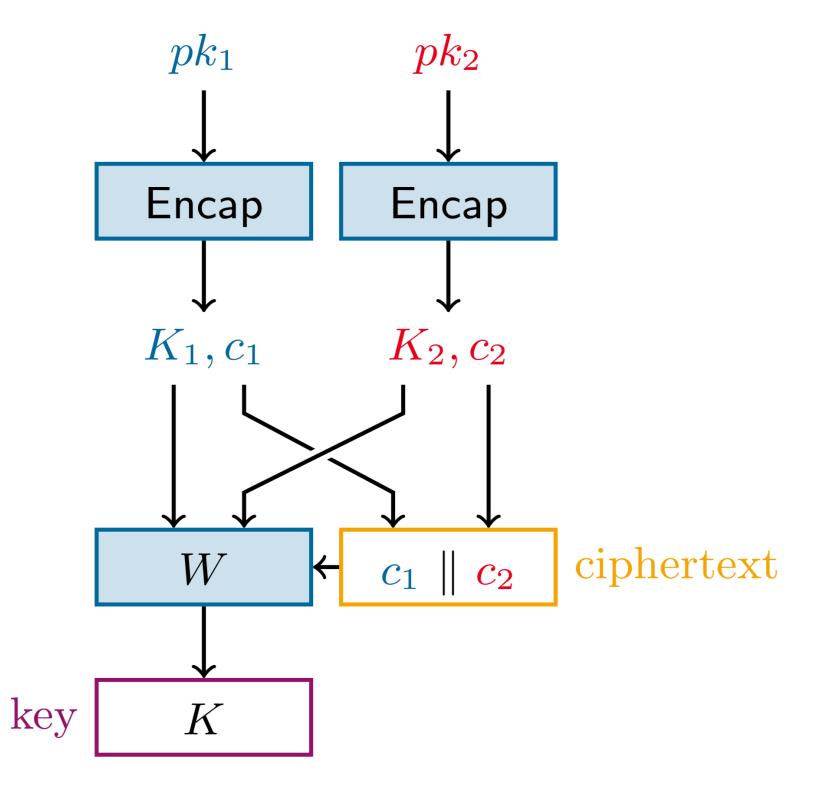
Kemeleon considered for adoption by CFRG

https://datatracker.ietf.org/doc/draft-veitch-kemeleon/

(more variants: no rejection, deterministic, ...)

Hybrid KEMs

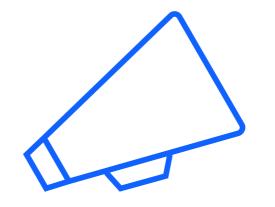
Parallel Combiner



TLS 1.3 hybrid, HPKE Xyber, XWing, ...

- Hybrid IND-CCA security
- **X** Hybrid Obfuscation

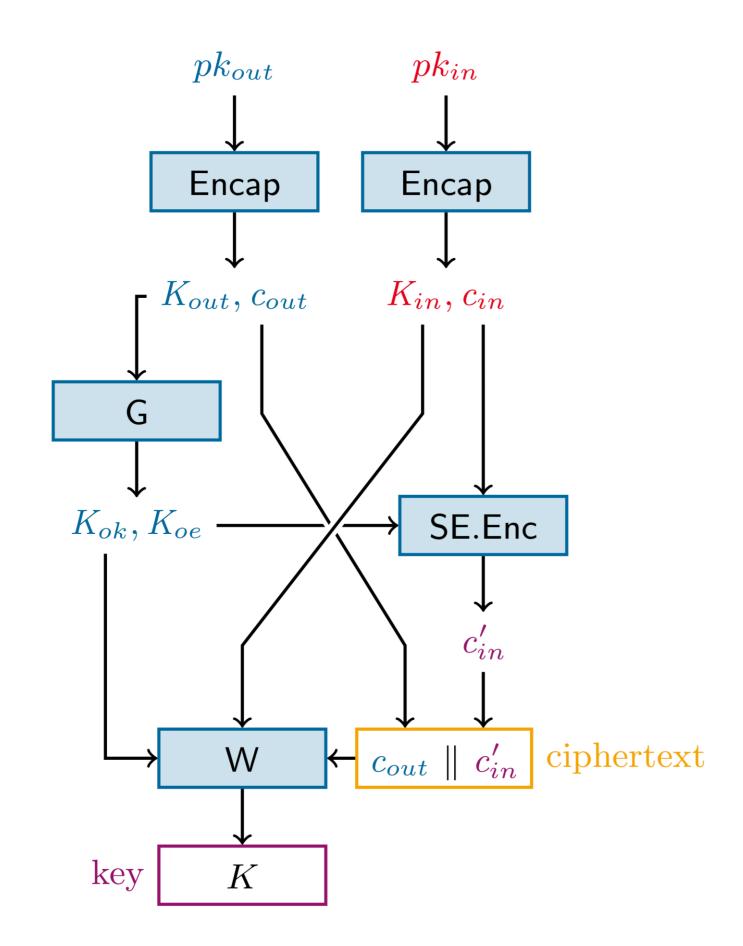
Hybrid Obfuscated KEMs



More details?

→ Shannon & Michael's talk @ RWC (Thu morning, PQ Deployment session)

OEINC



Outer-encrypts-inner nested combiner

- Hybrid IND-CCA security
- Hybrid Obfuscation
- ✓ Low overhead: 1 PRG + 1 XOR

example: outer = DH-Elligator (statistical)

inner = ML-Kemeleon (computational)

Use OEINC to build

- hybrid obfuscated key exchange
- hybrid PAKE (w/ adaptive corruptions)

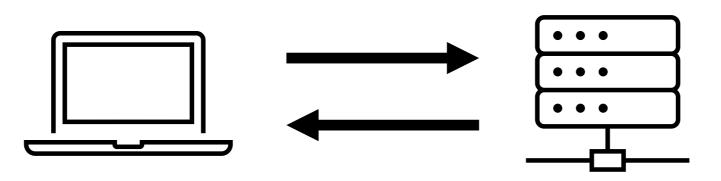
Cryptography Is Brittle

functionality



security

```
static OSStatus
SSLVerifySignedServerKeyExchange(SSLContext *ct
   SSLBuffer signedParams, uint8_t *signature,
   OSStatus
                    err;
   if ((err = SSLHashSHA1.update(&hashCtx, &se
        goto fail;
   if ((err = SSLHashSHA1.update(&hashCtx, &si
        goto fail; 
        goto fail; _
   if ((err = SSLHashSHA1.final(&hashCtx, &has
        goto fail;
fail:
    SSLFreeBuffer(&signedHashes);
    SSLFreeBuffer(&hashCtx);
    return err;
```



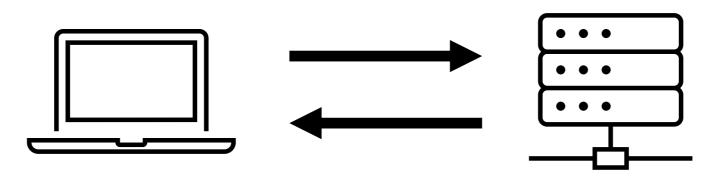
Cryptography Is Brittle

functionality



security

```
static OSStatus
SSLVerifySignedServerKeyExchange(SSLContext *ct
    SSLBuffer signedParams, uint8_t *signature,
    OSStatus
                    err;
    if ((err = SSLHashSHA1.update(&hashCtx, &se)
        goto fail;
    if ((err = SSLHashSHA1.update(&hashCtx, &si
        goto fail; \
        goto fail; _
    if ((err = SSLHashSHA1.final(&hashCtx, &has
        goto fail;
fail:
    SSLFreeBuffer(&signedHashes);
    SSLFreeBuffer(&hashCtx);
    return err;
```



Algorithm 18 ML-KEM.Decaps_internal(dk, c)

- 5: $m' \leftarrow \text{K-PKE.Decrypt}(dk_{PKF}, c)$
- 6: $(K',r') \leftarrow \mathsf{G}(m'\|h)$
- 7: $\bar{K} \leftarrow \mathsf{J}(z\|c)$
- 8: $c' \leftarrow \text{K-PKE.Encrypt}(ek_{PKE}, m', r')$



- 9: if $c \neq c'$ then
- $K' \leftarrow \bar{K}$
- 11: **end if**
- 12: return K'

FO transform

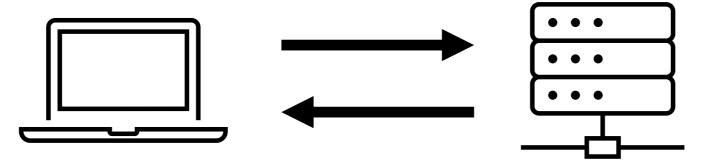
Cryptography Is Brittle

Can we tie **security** to **basic functionality**?

functionality



static OSStatus SSLVerifySignedServerKeyExchange(SSLContext *ct SSLBuffer signedParams, uint8_t *signature, **OSStatus** err; if ((err = SSLHashSHA1.update(&hashCtx, &se goto fail; if ((err = SSLHashSHA1.update(&hashCtx, &si goto fail; ___ goto fail; if ((err = SSLHashSHA1.final(&hashCtx, &has) goto fail; fail: SSLFreeBuffer(&signedHashes); SSLFreeBuffer(&hashCtx); return err;



security

```
int PQCLEAN_HQC128_CLEAN_crypto_kem_dec(uint8_t *ss, const uint8_t *ct, const uint8_t *sk) {
 86
 87
           uint8 t result;
           uint64_t u[VEC_N_SIZE_64] = \{0\};
 89
           uint64_t v[VEC_N1N2_SIZE_64] = \{0\};
           const uint8_t *pk = sk + SEED_BYTES;
 91
           uint8_t sigma[VEC_K_SIZE_BYTES] = {0};
 92
           uint8_t theta[SHAKE256_512_BYTES] = {0};
           uint64_t u2[VEC_N_SIZE_64] = {0};
 93
 94
           uint64_t v2[VEC_N1N2_SIZE_64] = \{0\};
 95
           uint8_t mc[VEC_K_SIZE_BYTES + VEC_N_SIZE_BYTES + VEC_N1N2_SIZE_BYTES] = {0};
           uint8_t tmp[VEC_K_SIZE_BYTES + PUBLIC_KEY_BYTES + SALT_SIZE_BYTES] = {0};
 97
           uint8_t *salt = tmp + VEC_K_SIZE_BYTES + PUBLIC_KEY_BYTES;
 99
            shake256incctx shake256state;
100
101
           // Retrieving u, v and d from ciphertext
102
           PQCLEAN_HQC128_CLEAN_hqc_ciphertext_from_string(u, v, salt, ct);
103
104
           // Decrypting
105
           result = PQCLEAN_HQC128_CLEAN_hqc_pke_decrypt(m, sigma, u, v, sk);
106
107
           // Computing theta
108
           memcpy(tmp + VEC_K_SIZE_BYTES, pk, PUBLIC_KEY_BYTES);
109
           PQCLEAN_HQC128_CLEAN_shake256_512_ds(&shake256state, theta, tmp, VEC_K_SIZE_BYTES + PUBLIC_
110
111
           // Encrypting m'
112
           PQCLEAN_HQC128_CLEAN_hqc_pke_encrypt(u2, v2, m, theta, pk);
113
114
           // Check if c != c'
115
           result |= PQCLEAN_HQC128_CLEAN_vect_compare((uint8_t *)u, (uint8_t *)u2, VEC_N_SIZE_BYTES);
           result |= PQCLEAN_HQC128_CLEAN_vect_compare((uint8_t *)v, (uint8_t *)v2, VEC_N1N2_SIZE_BYTE
116
117
           result = (uint8_t) (-((int16_t) result) >> 15);
118
119
120
           for (size_t i = 0; i < VEC_K_SIZE_BYTES; ++i) {</pre>
121
                mc[i] = (m[i] & result) ^ (sigma[i] & ~result);
122
```

Verifiable Decapsulation

```
\frac{\mathsf{Decaps}(\mathsf{sk},c)}{\mathsf{o5}\ m' \leftarrow \mathsf{Dec}(\mathsf{sk},c)}
\mathsf{o6}\ (c' \qquad) \leftarrow \mathsf{Enc}(\mathsf{pk},m')
\mathsf{o7}\ \mathsf{check}\ c' = c
\mathsf{o8}\ K' \leftarrow \mathsf{KDF}(m',\mathsf{pk})
\mathsf{o9}\ \mathbf{return}\ K'
```

Verifiable Decapsulation

Enter: Confirmation Codes

building on ideas from [Fischlin-G'23]

$$\frac{\mathsf{Decaps}(\mathsf{sk},c)}{\mathsf{o5}\ m' \leftarrow \mathsf{Dec}(\mathsf{sk},c)}$$

$$\mathsf{o6}\ (c',\mathsf{cd'}) \leftarrow \mathsf{Enc}(\mathsf{pk},m')$$

$$\mathsf{o7}\ \mathsf{check}\ c' = c$$

$$\mathsf{o8}\ K' \leftarrow \mathsf{KDF}(m',\mathsf{pk},\mathsf{cd'})$$

$$\mathsf{o9}\ \mathbf{return}\ K'$$

Idea: faulty implementation of re-encryption \rightarrow noticeable KEM correctness failure

ML-KEM with Confirmation Codes

ML-KEM ciphertext compression → lost entropy



leverage lost entropy for confirmation code

Using 12-20 bytes of confirmation code

detect faulty re-encryption in ML-KM-512/768/1024

by single test w/ probability $^{\sim}1/3$

at ≤ 3.4% performance overhead

```
Algorithm 14 K-PKE. Encrypt (ek_{PKE}, m, r)
Uses the encryption key to encrypt a plaintext message using the randomness r.
Input: encryption key \operatorname{ek}_{\mathsf{PKE}} \in \mathbb{B}^{384k+32}.
Input: message m \in \mathbb{B}^{32}.
Input: randomness r \in \mathbb{B}^{32}.
Output: ciphertext c \in \mathbb{B}^{32(d_uk+d_v)}
  1: N \leftarrow 0
  \mathbf{2:} \ \hat{\mathbf{t}} \leftarrow \mathsf{ByteDecode}_{12}(\mathsf{ek}_{\mathsf{PKE}}[0:384k]) \quad \triangleright \ \mathsf{run} \ \mathsf{ByteDecode}_{12} \ k \ \mathsf{times} \ \mathsf{to} \ \mathsf{decode} \ \hat{\mathbf{t}} \in (\mathbb{Z}_q^{256})^k
  3: \rho \leftarrow \mathsf{ek}_{\mathsf{PKE}}[384k : 384k + 32]
                                                                                                              > extract 32-byte seed from ekpke
                                                                     \triangleright re-generate matrix \hat{\mathbf{A}} \in (\mathbb{Z}_q^{256})^{k \times k} sampled in Alg. 13
  4: for (i \leftarrow 0; i < k; i + +)
              for (j \leftarrow 0; j < k; j++)
                     \mathbf{A}[i,j] \leftarrow \mathsf{SampleNTT}(\rho \| j \| i)
                                                                                                \triangleright j and i are bytes 33 and 34 of the input
              end for
  8: end for
                                                                                                                                \triangleright generate \mathbf{y} \in (\mathbb{Z}_q^{256})^k
       for (i \leftarrow 0; i < k; i++)
              \mathbf{y}[i] \leftarrow \mathsf{SamplePolyCBD}_{n_{1}}(\mathsf{PRF}_{\eta_{1}}(r,N))
                                                                                                                \triangleright \mathbf{y}[i] \in \mathbb{Z}_{a}^{256} sampled from CBD
 12: end for
                                                                                                                              \triangleright generate \mathbf{e_1} \in (\mathbb{Z}_q^{256})^k
 13: for (k \leftarrow 0; i < k; i + +)
                                                                                                              \triangleright \mathbf{e_1}[i] \in \mathbb{Z}_q^{256} sampled from CBD
              \mathbf{e_1}[i] \leftarrow \mathsf{SamplePolyCBD}_{\eta_2}(\mathsf{PRF}_{\eta_2}(r,N))
16: end for
\textbf{17:} \ \ e_2 \leftarrow \mathsf{SamplePolyCBD}_{\eta_2}(\mathsf{PRF}_{\eta_2}(r,N))
                                                                                                                     \triangleright sample e_2 \in \mathbb{Z}_q^{256} from CBD
                                                                                                                                        \triangleright run NTT k times
 18: \hat{\mathbf{y}} \leftarrow \mathsf{NTT}(\mathbf{y})
 19: \mathbf{u} \leftarrow \mathsf{NTT}^{-1}(\mathbf{A}^{\top} \circ \hat{\mathbf{y}}) + \mathbf{e_1}
                                                                                                                                    \triangleright run NTT<sup>-1</sup> k times
 20: \mu \leftarrow \mathsf{Decompress} (\mathsf{ByteDecode}_1(m))
 21: v \leftarrow \mathsf{NTT}^{-1}(\hat{\mathbf{t}}^{\top} \circ \hat{\mathbf{y}}) + e_2 + \mu
                                                                                                   \triangleright encode plaintext m into polynomial v
 22: c_1 \leftarrow \mathsf{ByteEncode}_J (\mathsf{Compress}_J (\mathbf{u}))
                                                                                        \triangleright run ByteEncode<sub>d</sub> and Compress<sub>d</sub> k times
\mathbf{23:} \ \ c_2 \leftarrow \mathsf{ByteEncode}_{d_v}^{a_u}(\mathsf{Compress}_{d_v}^{a_u}(v))
24: \operatorname{cd} \leftarrow (\mathbf{u}[1][S], \dots, \mathbf{u}[k][S], v[S])
     \mathbf{return} \ \left( c = c_1 \| c_2, \ \mathsf{cd} \ \right)
```

Summary

(HYBRID) OBFUSCATION

Kemeleon: obfuscate ML-KEM pk/ctxt

– pk even 2.5% smaller

OEINC: hybrid KEM obfuscation

VERIFIABLE DECAPSULATION

functionality



security

ML-KEM: $12-20B \rightarrow detect prob. ~1/3$

HQC: $1B \rightarrow basic tests catch bug$

full versions @ IACR ePrint:

- Kemeleon: ia.cr/2024/1086

https://datatracker.ietf.org/doc/draft-veitch-kemeleon/

– hybrid OKEMs: ia.cr/2025/408

Verifiable Decaps: ia.cr/2025/450

Thank You!

mail@felixguenther.info